

**Outcome 3 – Topic 2**  
**Specific Heat Capacity**

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○ Specific heat capacity is the amount of energy required to raise the temperature of 1 gram of substance by 1°C.

- Iron has a specific heat capacity of 0.45 J/g °C

This means that it takes 0.45 Joules of incoming heat energy to raise 1 gram of iron by 1°C

This also means that if we were to allow 1 g of iron to cool down by 1°C, it would release 0.45 Joules of heat.

- Water has a specific heat capacity of 4.19 J/g °C

This means that it takes 4.19 Joules of incoming heat energy to raise the temperature of water by 1°C.

This also means that if we were to cool 1g of water down by 1°C, 4.19 Joules of energy would be released.

<http://www.youtube.com/watch?v=hyPLusD-tyM>

**Quantity of Thermal Energy, Q**

○ If we know the specific heat capacity of a substance, we can use the equation  $Q = mc\Delta t$  to find out exactly how much heat energy is being absorbed by a particular mass of a substance.

**Q = quantity of heat energy (Joules (J))**

**m = mass of substance (g)**

**c = specific heat capacity of the substance (J/g °C)**

$\Delta = \text{change in}$

**$\Delta t = \text{change in temperature (°C)}$**

**$\Delta t = \text{final temperature} - \text{initial/starting temperature}$**

**$\Delta t = t_f - t_i$**

So say we have 50g of water that is in a beaker on a hotplate. The temperature of this mass of water started at 20°C and rose to a final temperature of 50°C.

We know that it takes 4.19 J of energy to change 1 g of water by 1 °C, how much energy does it take to raise 50 g of water by 30 °C?

$$\begin{aligned}
 Q &= ?? \\
 m &= 50 \text{ g} \\
 c &= 4.19 \text{ J/g } ^\circ\text{C} \\
 \Delta t &= t_f - t_i \\
 &= 50^\circ\text{C} - 20^\circ\text{C} \\
 &= 30^\circ\text{C}
 \end{aligned}$$

$$50 \cancel{\text{g}} \times \frac{4.19 \text{ J}}{\cancel{\text{g}} \cdot \cancel{^\circ\text{C}}} \times 30 \cancel{^\circ\text{C}}$$

$$\begin{aligned}
 Q &= mc\Delta t \\
 &= 50 \text{ g} \times 4.19 \text{ J/g } ^\circ\text{C} \times 30^\circ\text{C} \\
 &= 6285 \text{ J} \\
 &= 6.3 \times 10^3 \text{ J} \quad \boxed{6.3 \text{ kJ}}
 \end{aligned}$$

### Rearranging Equations

If we are given the values for any 3 of the four variables in the  $Q = mc\Delta t$  equation above, we can solve for the missing one.

To do this we must be able to rearrange the equation properly to solve for the unknown variable

$$Q = mc\Delta t$$

Solve for m,  $m = Q / (c \Delta t)$

Solve for c,  $c = Q / (m \Delta t)$

Solve for Δt,  $\Delta t = Q / (m c)$

Examples

1. Calculate the amount of thermal energy required to raise the temperature of 3.0 kg of aluminum from 20.0 to 80.0°C. The specific heat capacity of aluminum is 0.897 J/g °C.

$$\begin{aligned}
 Q &= ? \\
 m &= 3.0 \text{ kg} \\
 c &= 0.897 \text{ J/g} \cdot \text{°C} \\
 \Delta t &= 80.0 - 20.0 \\
 &= 60.0 \text{ °C}
 \end{aligned}$$

$$\begin{aligned}
 Q &= m c \Delta t \\
 &= (3000 \text{ g}) (0.897 \text{ J/g} \cdot \text{°C}) (60.0 \text{ °C}) \\
 &= 161460 \text{ J} \quad \boxed{1.6 \times 10^5 \text{ J}}
 \end{aligned}$$

2. When 60.0 J of energy is added to a mass of copper, the temperature of the copper increases by 10.4 °C. The specific heat capacity of copper is 0.385 J/g °C. What mass of copper was heated?

$$\begin{aligned}
 Q &= 60.0 \text{ J} \\
 m &= ? \\
 c &= 0.385 \text{ J/g} \cdot \text{°C} \\
 \Delta t &= 10.4 \text{ °C}
 \end{aligned}$$

$$\begin{aligned}
 Q &= m c \Delta t \\
 60.0 \text{ J} &= m (0.385 \text{ J/g} \cdot \text{°C}) (10.4 \text{ °C}) \\
 60.0 \text{ J} &= \boxed{m} (4.004 \text{ J/g}) \\
 \frac{60.0 \text{ J}}{4.004 \text{ J/g}} &= \frac{m}{1} \\
 m &= 14.985 \dots \text{ g} \\
 &= \boxed{15.0 \text{ g}}
 \end{aligned}$$

3. A 2.50 g mass of iron is at 24.0°C. Determine the final temperature of the iron after it absorbs 13.5 J of thermal energy. The specific heat capacity of iron is 0.449 J/g °C.

$$\begin{aligned}
 Q &= 13.5 \text{ J} \\
 m &= 2.50 \text{ g} \\
 c &= 0.449 \text{ J/g} \cdot \text{°C} \\
 \Delta t &= ?
 \end{aligned}$$

$$\begin{aligned}
 Q &= m c \Delta t \\
 13.5 \text{ J} &= (2.50 \text{ g}) (0.449 \text{ J/g} \cdot \text{°C}) (\Delta t) \\
 13.5 \text{ J} &= (1.1225 \text{ J/°C}) \Delta t \\
 \Delta t &= 12.0267 \dots \text{ °C} \\
 t_f &= 24.0 + 12.0 \dots \\
 &= \boxed{36.0 \text{ °C}}
 \end{aligned}$$

4. The heat capacity of water is 4.19 J/g °C, the heat capacity of aluminum is 0.897 J/g °C. 1.00 g of water and 1.00 g of aluminum are both heated from 20°C to 50°C.

a. Which substance will have absorbed more energy? Explain

b. Which will reach 50°C first? Explain

c. Which will cool down slower after the heat source is taken away? Explain